## PANUA PARDISO Version 8.2

CALL PARDISO (PT, MAXFCT, MNUM, MTYPE, PHASE, N, A, IA, JA,
1 PERM, NRHS, IPARM, MSGLVL, B, X, ERROR, DPARM)

| Name | Type | Description | Input/Output |
| :---: | :---: | :---: | :---: |
| PT (64) | INT | Internal memory address pointer. | I/O |
| MAXFCT | INT | Number of numerical factorizations in memory. | I |
| MNUM | INT | Actual matrix to factorize. | I |
| MTYPE | INT | Matrix type. | I |
|  | $\begin{gathered} 1 \\ 2 \\ -2 \\ 11 \end{gathered}$ | real and structurally symmetric, supernode pivoting real and symmetric positive definite real and symmetric indefinite, diagonal or Bunch-Kaufman pivoting real and nonsymmetric, complete supernode pivoting |  |
|  | $\begin{gathered} 3 \\ 4 \\ -4 \\ 6 \\ 13 \end{gathered}$ | complex and structurally symmetric, supernode pivoting complex and hermitian positive definite complex and hermitian indefinite, diagonal or Bunch-Kaufman pivoting complex and symmetric complex and nonsymmetric, supernode pivoting |  |
| PHASE | INT | Solver Execution Phase. | I |
|  | $\begin{gathered} \hline 11 \\ 12 \\ 13 \\ 22 \\ -22 \\ 23 \\ 33 \end{gathered}$ | Analysis <br> Analysis, Numerical Factorization <br> Analysis, Numerical Factorization, Solve, Iterative Refinement <br> Numerical Factorization <br> Selected Inversion <br> Numerical Factorization, Solve, Iterative Refinement <br> Solve, Iterative Refinement |  |
|  | $\begin{gathered} -1 \\ 0 \end{gathered}$ | Release all internal memory for all matrices Release memory for matrix number MNUM |  |
| N | INT | Number of equations. | I |
| A (*) | R/C | Matrix values. | I |
| IA (N+1) | INT | Beginning of each row. | I |
| JA (*) | INT | Column indices. | I |
| PERM (N) | INT | User permutation. | I |
| NRHS | INT | Number of right-hand sides. | I |
| IPARM (64) | INT | Control parameters. | I/O |
| MSGLVL | INT | Message level. | I |
|  | $\begin{aligned} & 0 \\ & 1 \end{aligned}$ | No output. <br> Output statistical information |  |
| B (N, NRHS) | R/C | Right-hand sides. | I/O |
| X (N, NRHS) | R/C | Solution vectors (see IPARM(6)). | O |
| ERROR | INT | Error indicator. | O |
| DPARM (64) | REAL | Control parameters for iterative solver | I/O |

Table 1: Overview of subroutine arguments.

| Name | Description |  |
| :---: | :---: | :---: |
| IPARM(1) | Use default options. |  |
|  | 0 | Set all entries to their default values except IPARM(3). |
| IPARM(2) | Use METIS reordering. |  |
|  | $\begin{aligned} & \hline 0 \\ & 2^{*} \\ & 3 \\ & 4 \end{aligned}$ | Do not use METIS. <br> Use METIS nested dissection reordering. <br> Use METIS51 nested dissection reordering. <br> Use AMD ordering. |
| IPARM(3) | Number of processors. |  |
|  | $p$ | Number of OpenMP threads. This must be identical or slightly larger to the environment variable OMP_NUM_THREADS. |
| IPARM(4) | Do preconditioned CGS iterations (see description). Default is 0 . |  |
| IPARM(5) | Use user permutation. |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Do not use user perm. <br> Use the permutation provided in argument PERM. |
| IPARM(6) | Solution on X / B |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Write solution to $X$ Write solution to B |
| IPARM(8) | Max. numbers of iterative refinement steps. |  |
|  | $\mathrm{k}=0^{*}$ | The solver automatically performs two steps of iterative refinement when perturbed pivots are obtained during the numerical factorization. The number of executed iterations is reported in IPARM(7). |
|  | $k>0$ | Maximum number of iterative refinement steps that the solver performs. The solver performs not more than the absolute value of IPARM (8) steps of iterative refinement. The solver might stop the process before the maximum number of steps if (1) a satisfactory level of accuracy of the solution in terms of backward error is achieved, or (2) or if it determines that the required accuracy cannot be reached. In this case the solver returns -4 in the error parameter. The number of executed iterations is reported in IPARM(7). |
|  | $k<0$ | Maximum number of iterative refinement steps with a negative sign. Unlike the case above the accumulation of the residuum uses extended precision real and complex data types. The number of iterative refinement steps is reported in IPARM(7). |
|  | $\mathrm{k}=-99$ | no iterative refinement for all matrices. |
| IPARM(9) | Tolerance level for the relative residual. |  |
|  | 0* | If set to zero, default checks are used to determine when to stop the iterations (see IPARM (8) description) |
|  | k | Tolerance level for the relative residual in the iterative refinement process. If set to a non-zero value, an additional criterion is used for stopping the iterative refinement: $\left.\\|r\\|_{2} /\\|b\\|_{2}<10^{-I P A R M(9)}\right)$ ). |
| $\operatorname{IPARM}(10)$ | eps pivot (perturbation $10^{-k}$ ). |  |
|  | $\begin{aligned} & 13^{*} \\ & 8^{*} \end{aligned}$ | Default for nonsymmetric matrices Default for symmetric indefinite matrices |

Table 2: Overview of input IPARM control parameters. An asterisk $\left(^{*}\right)$ indicates the default value.

| Name | Description |  |
| :---: | :---: | :---: |
| $\operatorname{IPARM}(11)$ | Use (non-) symmetric scaling vectors. |  |
|  | $\begin{aligned} & 0 \\ & 1^{*} \\ & 0^{*} \end{aligned}$ | Do not use. <br> Use (nonsymmetric matrices). <br> Do not use (symmetric matrices). |
| $\operatorname{IPARM}(12)$ | Solve transposed matrix. |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Do normal solve. <br> Do solve with transposed matrix. |
| $\operatorname{IPARM}(13)$ | Improved accuracy using (non-)symmetric matchings |  |
|  | $\begin{aligned} & 0 \\ & 1^{*} \\ & 2 \\ & 0^{*} \end{aligned}$ | Do not use. <br> Use (nonsymmetric matrices). <br> Use a very robust method for symmetric indefinite matrices. <br> Do not use (symmetric matrices). |
| $\operatorname{IPARM}(18)$ | Number of nonzeros in LU. |  |
|  | $\begin{aligned} & 0 \\ & -1^{*} \end{aligned}$ | Do not determine. Will only be determined if -1 on entry. |
| $\operatorname{IPARM}(19)$ | Gflops for LU factorization. |  |
|  | $\begin{aligned} & 0^{*} \\ & -1 \end{aligned}$ | Do not determine. <br> Will only be determined if -1 on entry. Increases ordering time. |
| $\operatorname{IPARM}(21)$ | Pivoting for symmetric indefinite matrices. Default is 1. |  |
|  |  | $1 \times 1$ Diagonal Pivoting <br> $1 \times 1$ and $2 \times 2$ Bunch-Kaufman pivoting. |
| $\operatorname{IPARM}(24)$ | Parallel Numerical Factorization |  |
|  | $\begin{aligned} & 0 \\ & 1^{*} \end{aligned}$ | Do one-level parallel scheduling. Do two-level parallel scheduling. |
| $\operatorname{IPARM}(25)$ | Parallel Forward/Backward Solve |  |
|  | $\begin{aligned} & \hline 0 \\ & 1^{*} \end{aligned}$ | Do sequential solve. Do parallel solve. |
| IPARM(26) | Partial Forward/Backward Solve |  |
|  | $\begin{aligned} & \hline 0^{*} \\ & 1 \\ & 2 \end{aligned}$ | Do forward/backward solve with $L$ and $U$. <br> Do forward solve with $L$ or $U^{T}$. <br> Do backward solve with $U$ or $L^{T}$. |
| IPARM(28) | Parallel METIS reordering |  |
|  |  | Do sequential METIS reordering. Do parallel METIS reordering. |
| IPARM(29) | 32-bit/64-bit IEEE accuracy |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Use 64-bit IEEE accuracy. Use 32-bit IEEE accuracy. |
| IPARM(30) | Contr <br> $0^{*}$ <br> 1 | ol size of supernodes <br> Use default configuration. Use use configuration. |

Table 3: Overview of input IPARM control parameters. An asterisk ( ${ }^{*}$ ) indicates the default value.

| Name | Description |  |
| :---: | :---: | :---: |
| IPARM(31) | Partial solve for sparse right-hand sides and sparse solutions |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Compute all components in the solution vector. Compute only a few selected in the solution vector. |
| IPARM(32) | Use the multi-recursive iterative linear solver |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Use sparse direct solver. <br> Use multi-recursive iterative solver. |
| IPARM(33) | Determinant for a matrices |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | Do not compute determinant. Compute determinant. |
| IPARM(34) | Identical solution independent on the number of processors |  |
|  | $\begin{aligned} & 0^{*} \\ & 1 \end{aligned}$ | No identical parallel results. Identical parallel results |
| IPARM(36) | Selected inversion for $A_{i j}^{-1}$ |  |
|  | $\begin{aligned} & \hline 0^{*} \\ & 1 \end{aligned}$ | Overwrite internal factor with inverse elements. Do not overwrite internal factor with inverse elements. |
| IPARM(37) | Selected inversion for $A_{i j}^{-1}$ for symmetric matrices |  |
|  | $0^{*}$ $1$ | Return inverse elements in upper triangular symmetric compressed CSR format (1-index based). <br> Return inverse elements in full symmetric compressed CSR format (1-index based). |
| IPARM(38) | Schur-complement computation |  |
|  | $\begin{aligned} & 0^{*} \\ & \mathrm{k} \end{aligned}$ | Indicates the numbers of rows/columns in $S$. Schur-complement matrix $S$ is a $k \times$ matrix. |
| IPARM(50) | Use out-of-core solver |  |
|  | $\begin{aligned} & 0^{*} \\ & >0 \end{aligned}$ | Use in-core solver Use out-of-core solver |
| IPARM(51) | Use parallel distributed-memory solver |  |
|  | $\begin{aligned} & \hline 0^{*} \\ & 1 \end{aligned}$ | Use OpenMP-threaded solver Use Mixed OpenMP-MPI solver |
| IPARM(52) | Number of nodes for distributed-memory solver |  |
|  | $\begin{aligned} & 1^{*} \\ & \mathrm{p} \end{aligned}$ | For OpenMP-threaded solver Use p compute nodes |
| IPARM(53) | Block size of Compression |  |
|  | $0^{*}$ $p$ | Normal CSR matrix format is expected on input, block compression is not used <br> Use p are the block size, block compression is used |

Table 4: Overview of input IPARM control parameters. An asterisk (*) indicates the default value.

| Name | Description |  |
| :---: | :---: | :---: |
| IPARM(54) | This parameter sets the number of dense columns for compression |  |
|  |  | Dense column compression is not used Use p dense columns at the end of the matrix, dense column compression is used |
| IPARM(55) | METIS 4.0.1 and METIS 5.1 ordering options |  |
|  |  | Default values in METIS <br> Other values can be used in METIS. Please see below. |
| IPARM(56) | Matching type in METIS |  |
|  | $\begin{aligned} & 1 \\ & 2 \\ & 3^{*} \end{aligned}$ | Random Matching (RM) <br> Heavy-Edge Matching (HEM, only for METIS 4.0.1). <br> Sorted Heavy-Edge Matching (SHEM) (Default). |
| IPARM(57) | Algorithm used during METIS initial partitioning. |  |
|  |  | Edge-based region growing (Default) Node-based region growing. |
| IPARM(58) | Algorithm used for METIS refinement. |  |
|  | $\begin{aligned} & 1 \\ & 2^{*} \end{aligned}$ | Two-sided node FM refinement. <br> One-sided node FM refinement (Default). |
| IPARM(59) | Used for METIS debugging purposes. |  |
|  | $\begin{aligned} & 0^{*} \\ & >0 \end{aligned}$ | no output. <br> output from METIS (statistics, etc, pleaser refer to the METIS manuals). |
| IPARM(60) | Compression of the graph in METIS. |  |
|  | $\begin{aligned} & 0^{*} \\ & >0 \end{aligned}$ | no compression. <br> compression, pleaser refer to the METIS manuals). |
| $\operatorname{IPARM}(61)$ | Removal of vertices with high degree in METIS |  |
|  | $\begin{aligned} & 0 \\ & \mathrm{p}^{*} \end{aligned}$ | Do not remove any vertices Removal o vertices |
| IPARM(62) | Trial number of separators. |  |
|  | $\begin{aligned} & 1^{*} \\ & \mathrm{k} \end{aligned}$ | only one trial Use $k$ trials |

Table 5: Overview of input IPARM control parameters. An asterisk ( ${ }^{*}$ ) indicates the default value.


Table 6: Overview of output IPARM/DPARM control parameters. An asterisk (*) indicates the default value.

| Error | Information |
| :---: | :--- |
| 0 | No error. |
| -1 | Input inconsistent. |
| -2 | Not enough memory. |
| -3 | Reordering problem. |
| -4 | Zero pivot, numerical fact. or iterative refinement problem. |
| -5 | Unclassified (internal) error. |
| -6 | Preordering failed (matrix types 11, 13 only). |
| -7 | Diagonal matrix problem. |
| -8 | 32-bit integer overflow problem. |
| -10 | No license file pardiso.lic found. |
| -11 | License is expired. |
| -12 | Wrong username or hostname. |
| -100 | Reached maximum number of Krylov-subspace iteration in iterative solver. |
| -101 | No sufficient convergence in Krylov-subspace iteration within 25 iterations. |
| -102 | Error in Krylov-subspace iteration. |
| -103 | Break-Down in Krylov-subspace iteration. |

Table 7: PARDISO Error codes.

